

Lecture 6 Edge Detection

COMP3204 Computer Vision

What are edges and how do we find them?



Book
pp
118 -
130

**Department of
Electronics and
Computer Science**

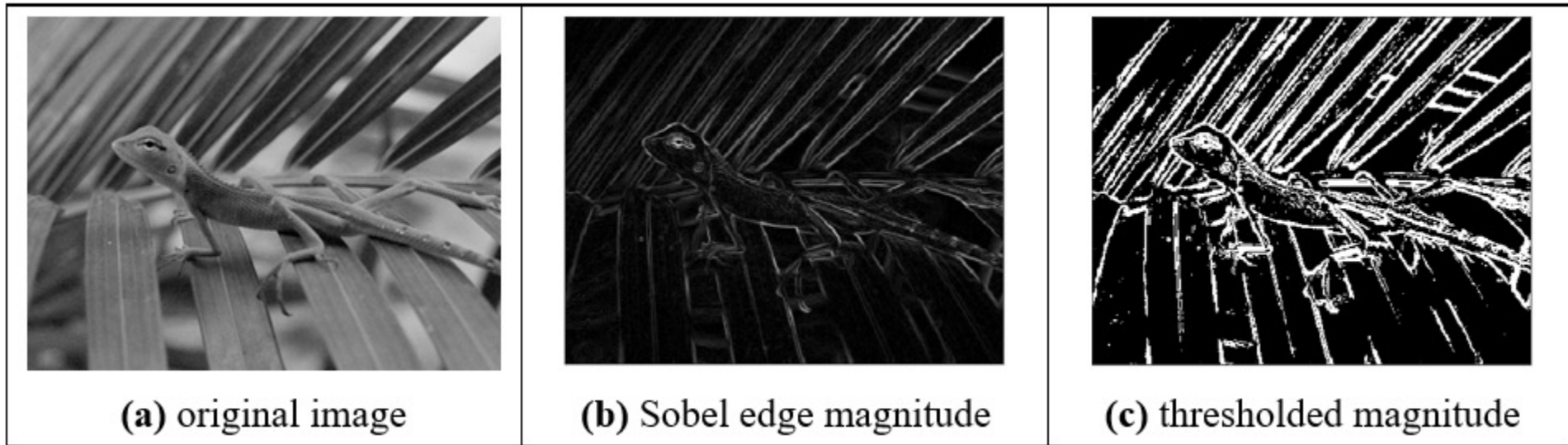
UNIVERSITY OF
Southampton
School of Electronics
and Computer Science

Content

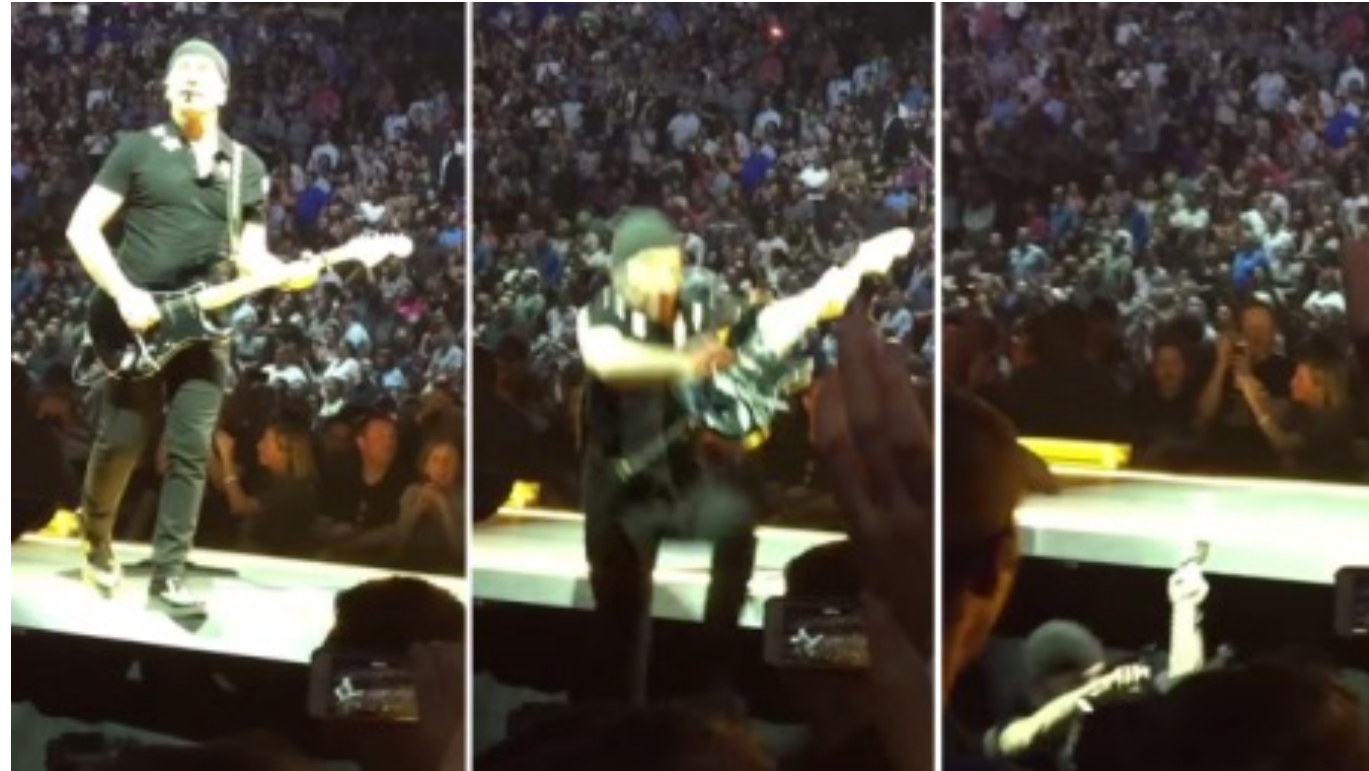
1. Differentiation/ differencing can be used to find edges of features
2. How can we improve the differencing process?

Edge detection

What is an **edge**? It's **contrast**

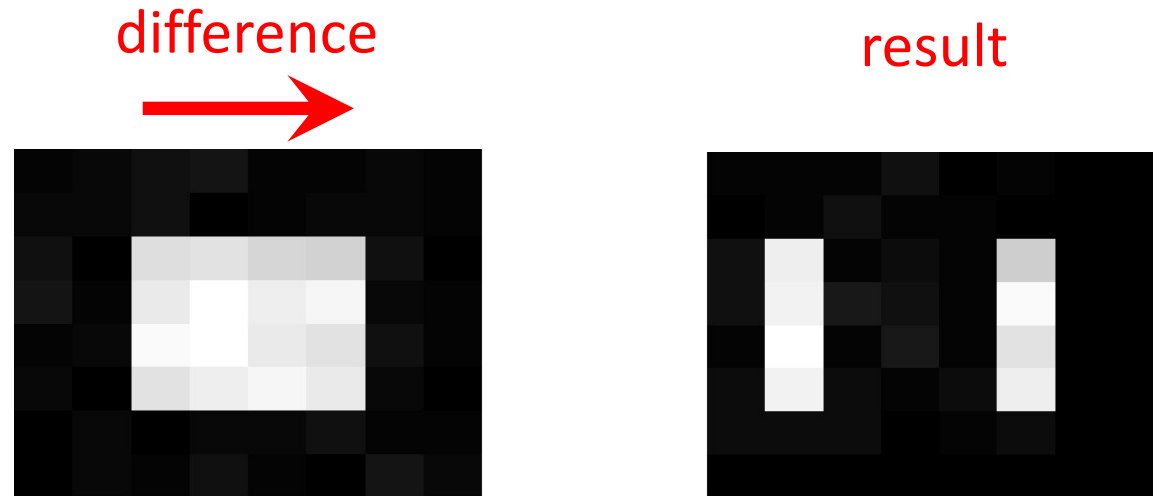


U2's Edge can't detect edges

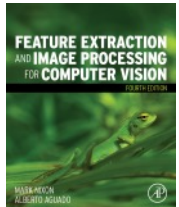


<http://metro.co.uk/2015/05/15/the-edge-falls-off-the-edge-of-the-stage-in-spectacular-style-during-u2s-world-tour-5199503/>

Horizontal differencing

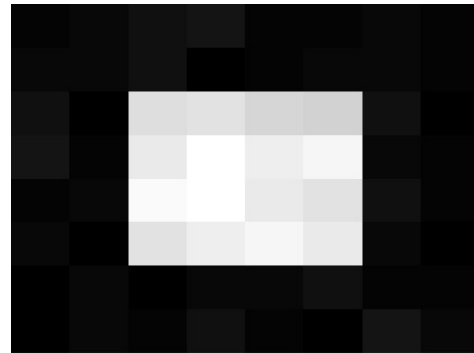


Horizontal differencing detects vertical edges



Vertical differencing

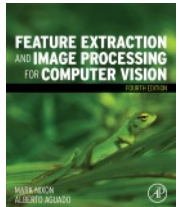
difference



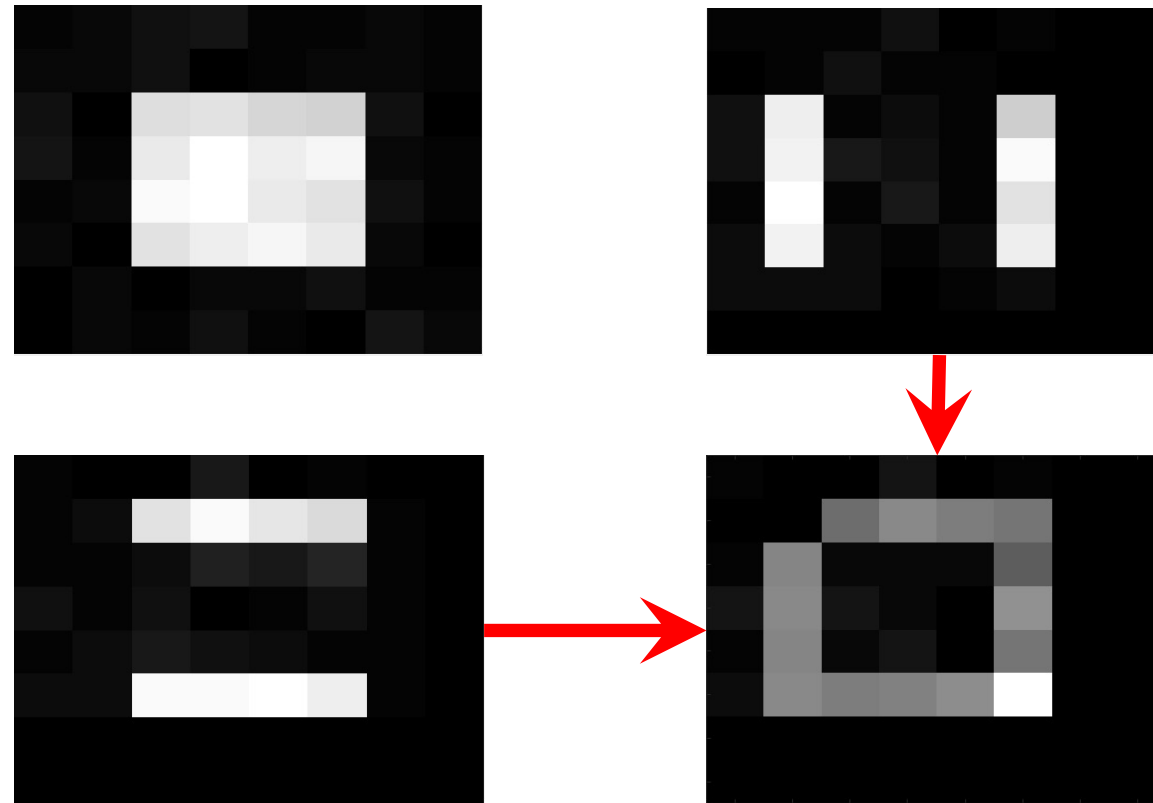
result



Vertical differencing detects horizontal edges



First order edge detection



Addition of
horizontal
and vertical



First order edge detection

- vertical edges, E_x

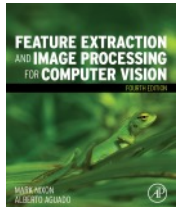
$$E_x_{x,y} = |P_{x,y} - P_{x+1,y}|$$

- horizontal edges, E_y

$$E_y_{x,y} = |P_{x,y} - P_{x,y+1}|$$

- vertical and horizontal edges

$$E_{x,y} = |2 \times P_{x,y} - P_{x+1,y} - P_{x,y+1}|$$



First order edge detection

Template

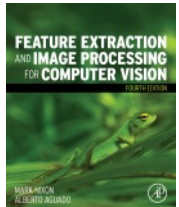
2	-1
-1	0

Code

```
function edge = basic_difference(image)

for x = 1:cols-2 %address all columns except border
    for y = 1:rows-2 %address all rows except border
        edge(y,x)=abs(2*image(y,x)-image(y+1,x)-image(y,x+1)); % Eq. 4.4
    end
end
```

How can we **improve** it?



Taylor series – evaluate $f(t + \Delta t)$

First approximation, original value

$$f(t + \Delta t) = f(t)$$

Second approximation, add gradient

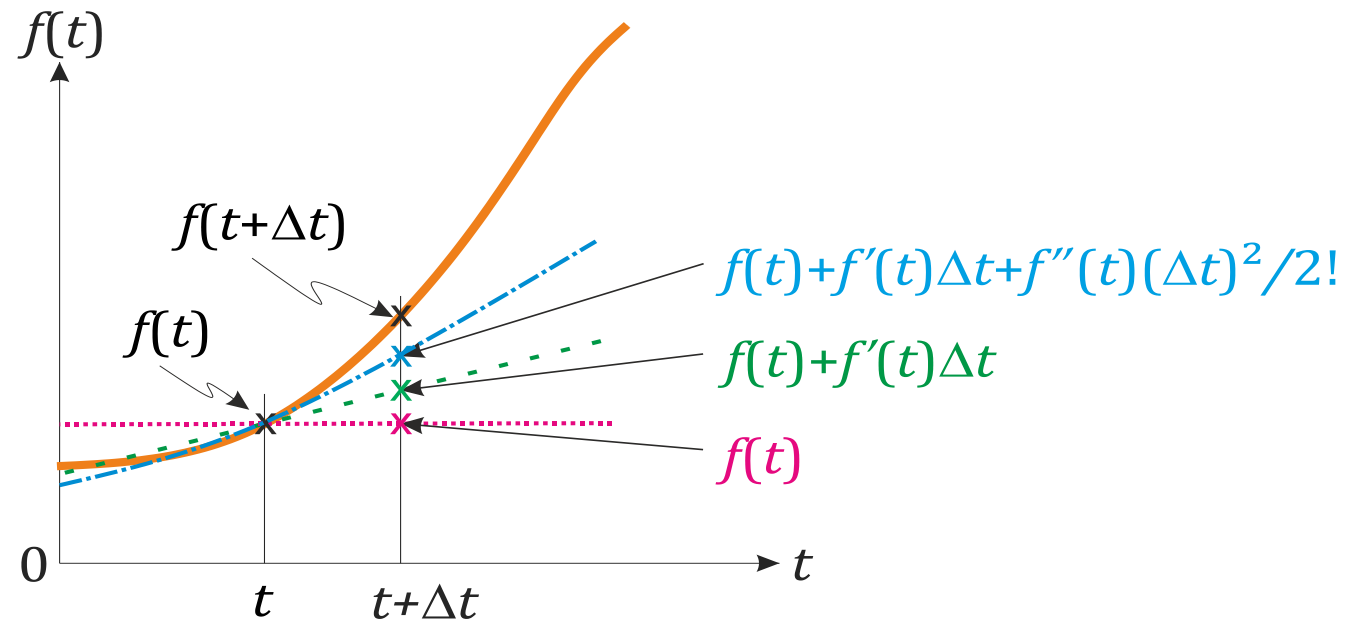
$$f(t + \Delta t) = f(t) + f'(t)\Delta t$$

Third approximation, add f''

$$f(t + \Delta t) = f(t) + f'(t)\Delta t + \frac{f''(t)}{2!}(\Delta t)^2$$

Taylor series

$$f(t + \Delta t) = f(t) + f'(t)\Delta t + \frac{f''(t)}{2!}(\Delta t)^2 + \frac{f'''(t)}{3!}(\Delta t)^3 + \dots + \frac{f^n(t)}{n!}(\Delta t)^n$$



Edge detection maths

Taylor expansion for $f(x + \Delta x)$ $f(x + \Delta x) = f(x) + \Delta x \times f'(x) + \frac{\Delta x^2}{2!} \times f''(x) + O(\Delta x^3)$ **A**

By rearrangement, $f'(x) = \frac{f(x + \Delta x) - f(x)}{\Delta x} - O(\Delta x)$

This is equivalent to $\mathbf{E}_{xx}_{x,y} = \left| \mathbf{P}_{x,y} - \mathbf{P}_{x-1,y} \right|$

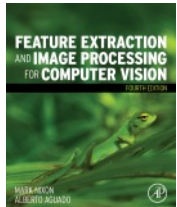
1	-1
---	----

Expand $f(x - \Delta x)$ $f(x - \Delta x) = f(x) - \Delta x \times f'(x) + \frac{\Delta x^2}{2!} \times f''(x) - O(\Delta x^3)$ **B**

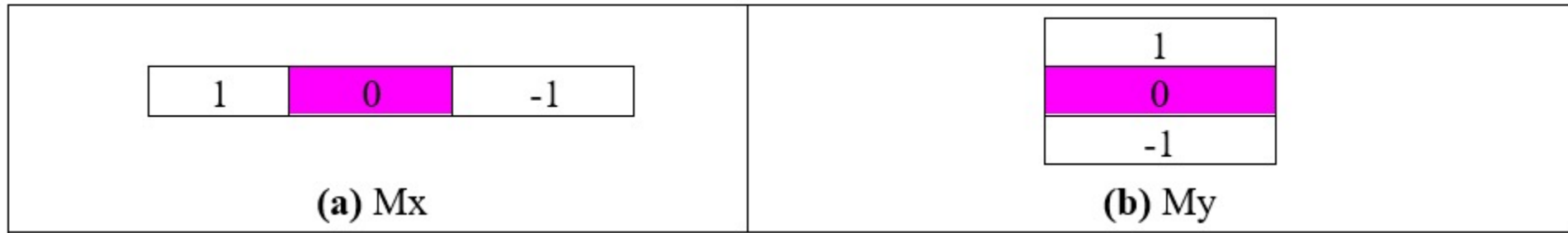
A - B $f'(x) = \frac{f(x + \Delta x) - f(x - \Delta x)}{2\Delta x} - O(\Delta x^2)$ $\mathbf{E}_{xx}_{x,y} = \left| \mathbf{P}_{x+1,y} - \mathbf{P}_{x-1,y} \right|$

If $\Delta x < 1$, this error is clearly smaller

1	0	-1
---	---	----



Templates for improved first order difference

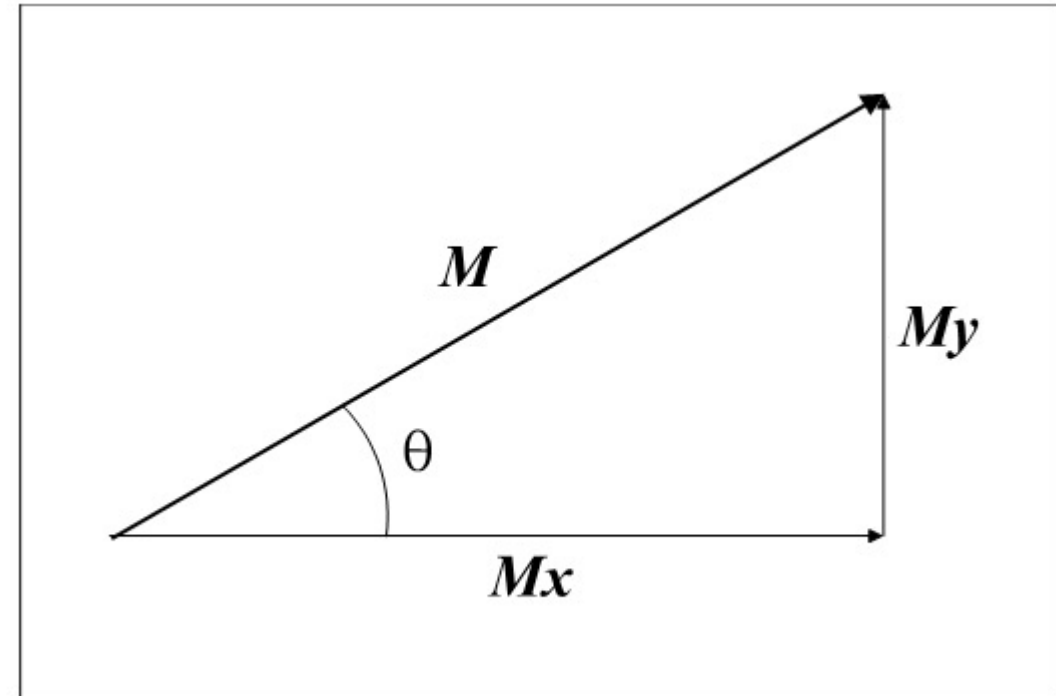


Edge Detection in Vector Format

Vectors have **magnitude** (strength) and **direction**

$$M = \text{magnitude} = \sqrt{M_x^2 + M_y^2}$$

$$\theta = \text{direction} = \tan^{-1} \left(\frac{M_y}{M_x} \right)$$



Templates for 3×3 Prewitt operator

Average improved horizontal and vertical operators over 3 rows/
columns to give **Prewitt** templates

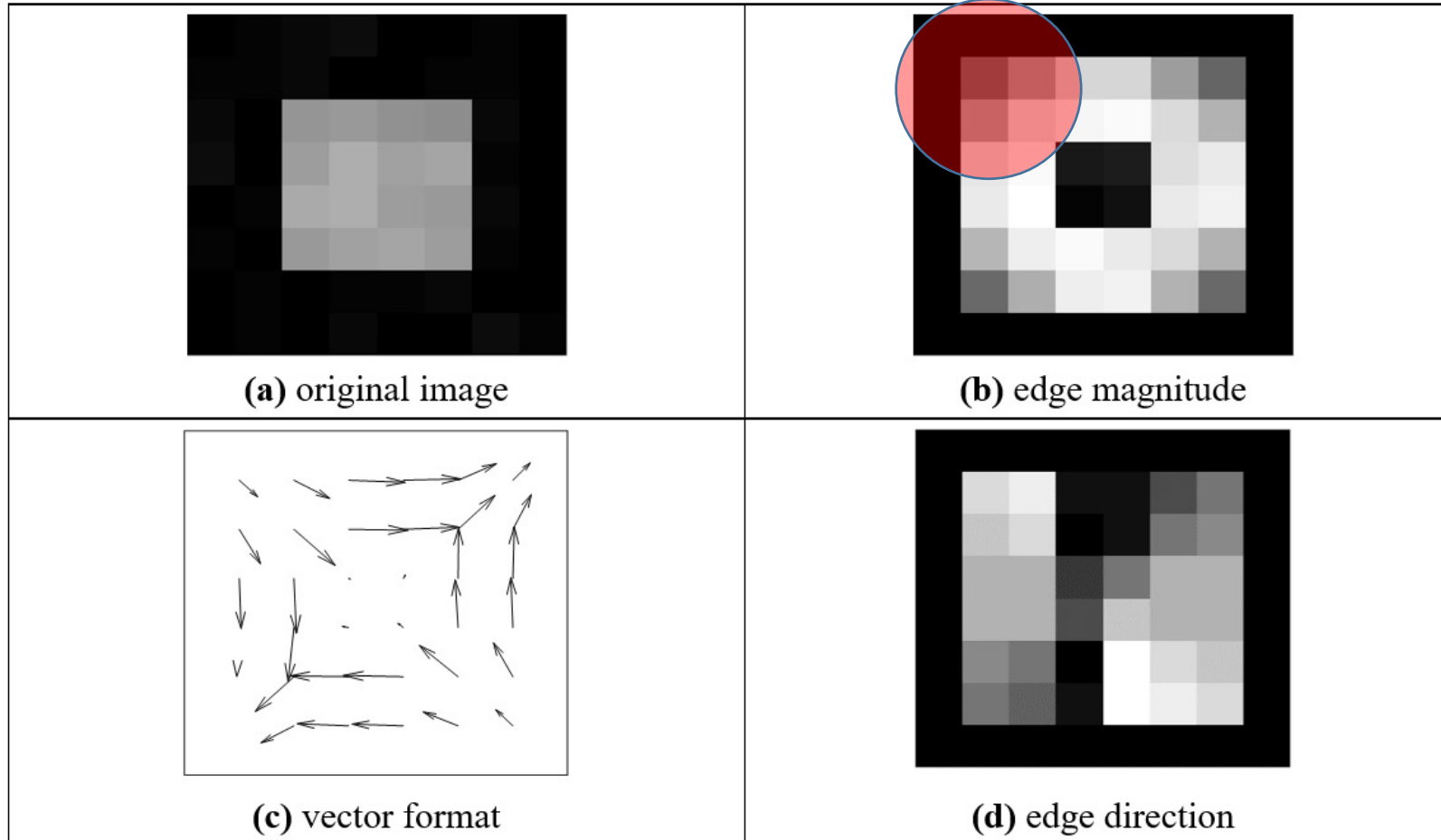
<table border="1"><tbody><tr><td>1</td><td>0</td><td>-1</td></tr><tr><td>1</td><td>0</td><td>-1</td></tr><tr><td>1</td><td>0</td><td>-1</td></tr></tbody></table>	1	0	-1	1	0	-1	1	0	-1	<table border="1"><tbody><tr><td>1</td><td>1</td><td>1</td></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>-1</td><td>-1</td><td>-1</td></tr></tbody></table>	1	1	1	0	0	0	-1	-1	-1
1	0	-1																	
1	0	-1																	
1	0	-1																	
1	1	1																	
0	0	0																	
-1	-1	-1																	
(a) M_x	(b) M_y																		

Edge magnitude and direction calculated for **centre** point



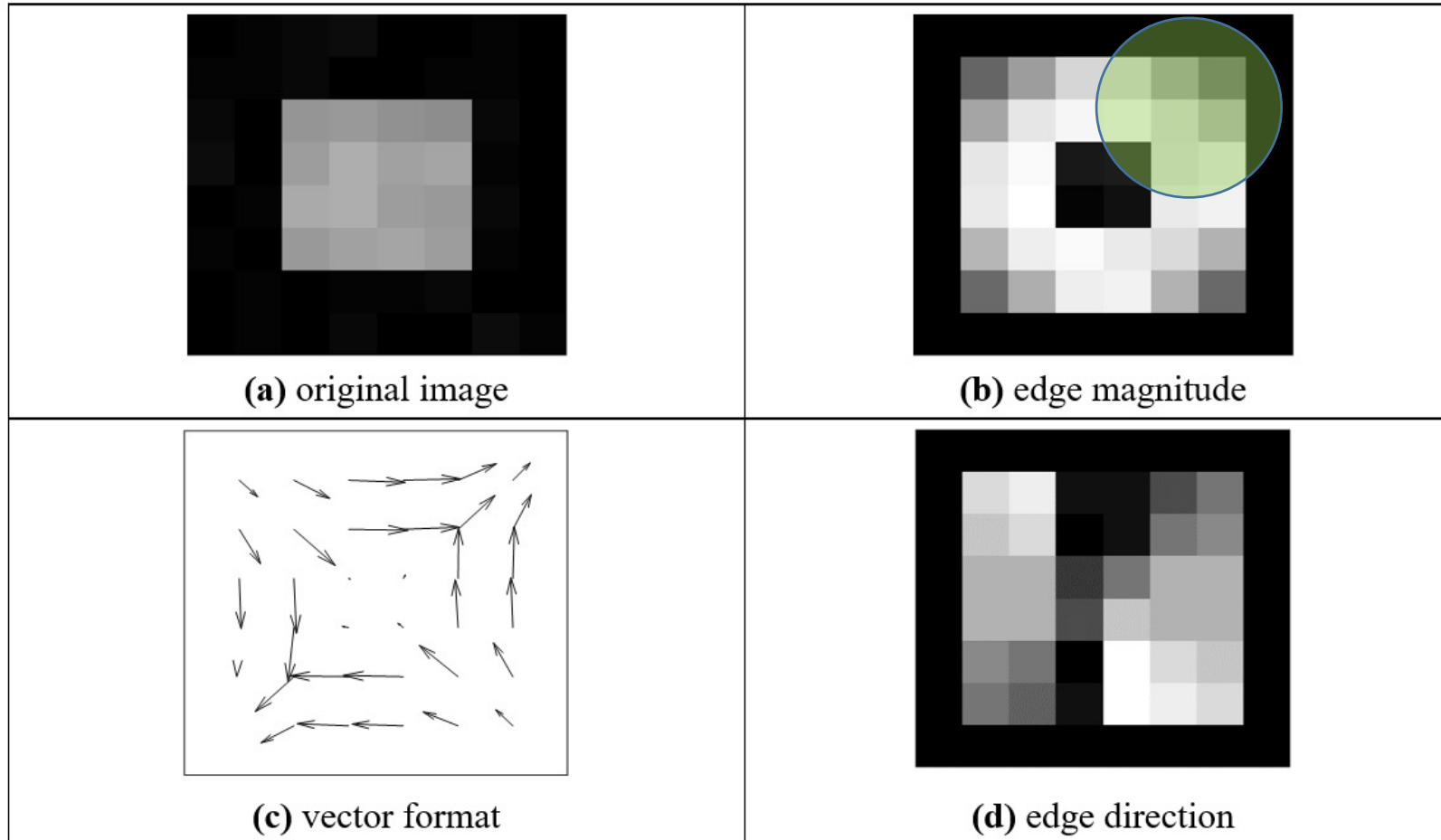
Applying the Prewitt Operator

No missing points



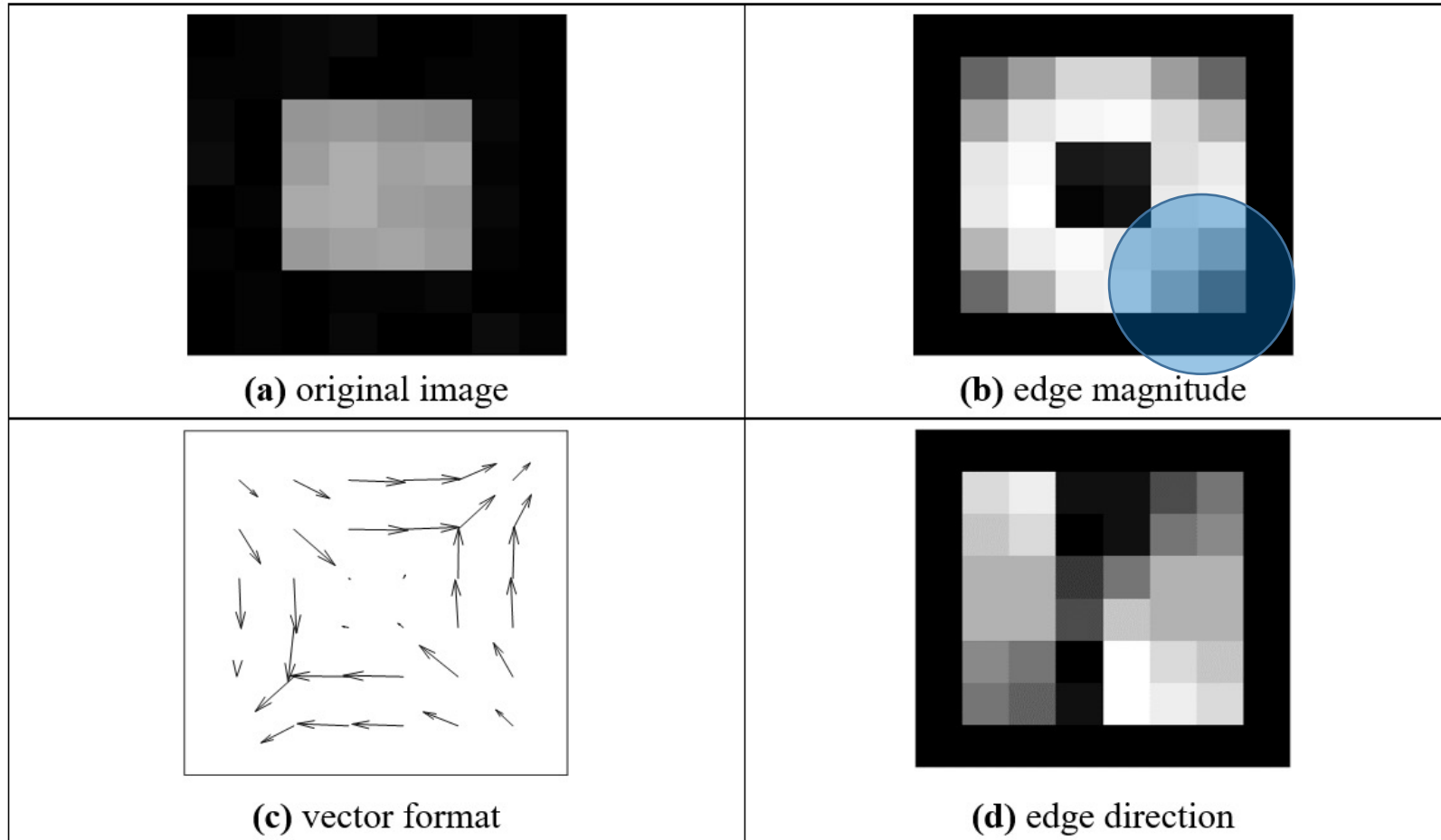
Applying the Prewitt Operator

Blurred edges



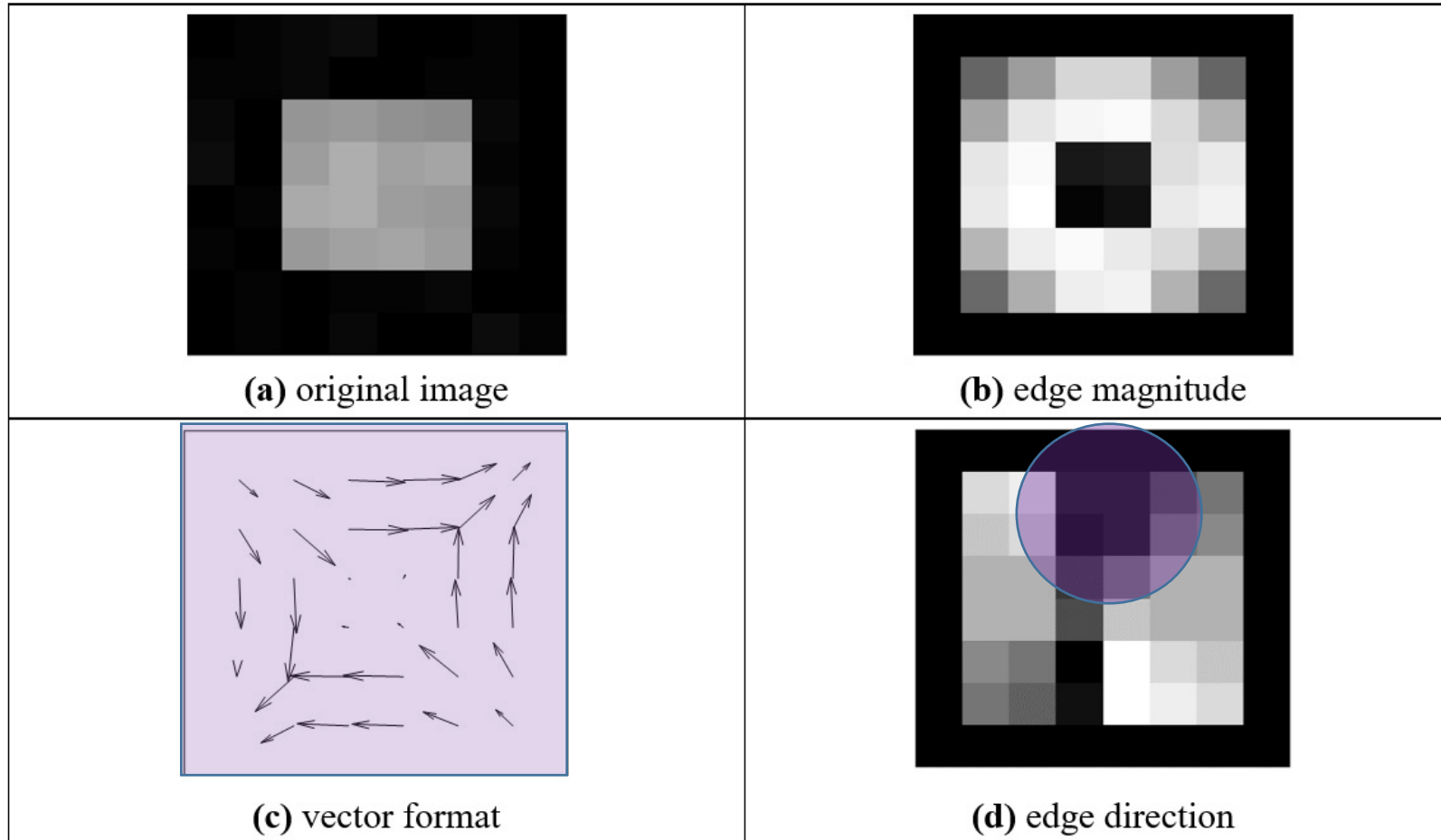
Applying the Prewitt Operator

No double points

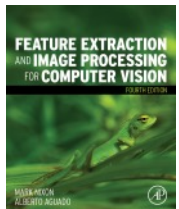


Applying the Prewitt Operator

Displaying gradients as an image communicates nothing



So use vectors

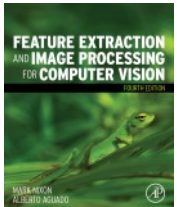


Templates for Sobel operator

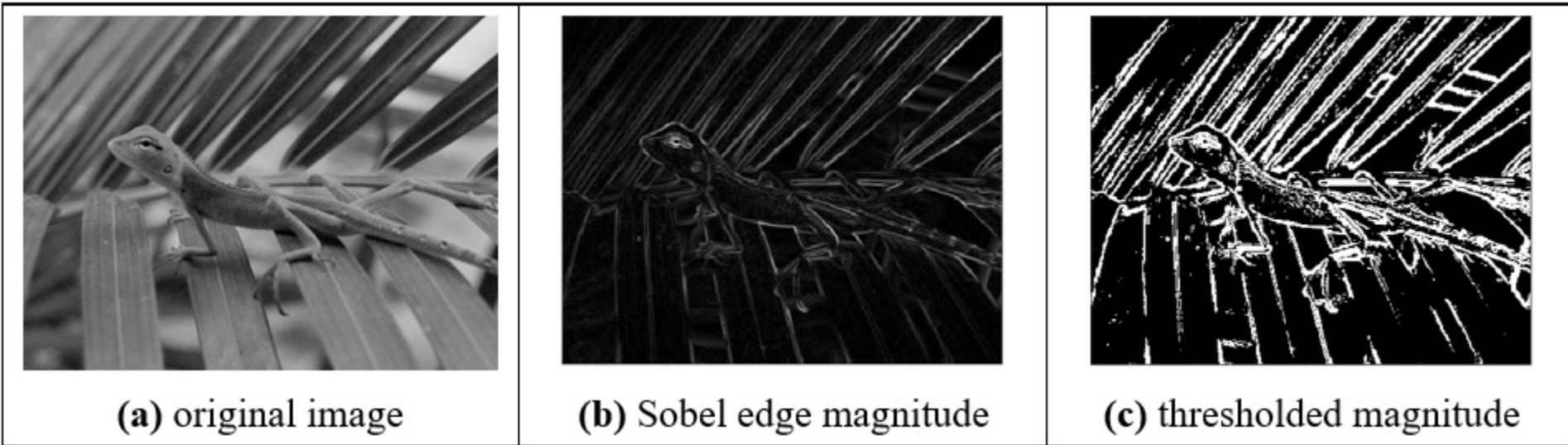
Sobel is most popular basic operator
Double the centre coefficients of Prewitt

<table border="1"><tr><td>1</td><td>0</td><td>-1</td></tr><tr><td>2</td><td>0</td><td>-2</td></tr><tr><td>1</td><td>0</td><td>-1</td></tr></table> <p>(a) M_x</p>	1	0	-1	2	0	-2	1	0	-1	<table border="1"><tr><td>1</td><td>2</td><td>1</td></tr><tr><td>0</td><td>0</td><td>0</td></tr><tr><td>-1</td><td>-2</td><td>-1</td></tr></table> <p>(b) M_y</p>	1	2	1	0	0	0	-1	-2	-1
1	0	-1																	
2	0	-2																	
1	0	-1																	
1	2	1																	
0	0	0																	
-1	-2	-1																	

WHY?



Applying Sobel operator



Generalising Sobel - use Pascal's triangle

1. Averaging

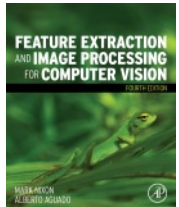
Window size

2			1		1					
3			1		2		1		Sobel 3×3	
4		1		3		3		1		
5	1		4		6		4		1	Sobel 5×5

2. Differencing

Window size

2			1		-1					
3			1		0		-1		Sobel 3×3	
4		1		1		-1		-1		
5	1		2		0		-2		-1	Sobel 5×5



Generalised Sobel

Generated by: averaging^T *(differencing)

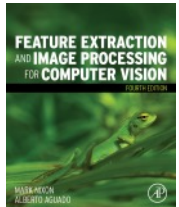
```
>> s=Sobel_templates(5)
```

```
s(:, :, 1) =
```

1	2	0	-2	-1
4	8	0	-8	-4
6	12	0	-12	-6
4	8	0	-8	-4
1	2	0	-2	-1

Main points so far

- 1 – differencing detects contrast and thus **edges**
 - 2 - can **improve** the differencing process (by maths!!)
 - 3 – **Sobel** is a good general purpose operator
- We shall go to more sophisticated methods, coming up next.



Filters for edge detection